

Name & ID: * $P_1 = D_3 \oplus D_5 \oplus D_7$ $P_2 = D_3 \oplus D_5 \oplus D_7$
 $P_2 = D_3 \oplus D_6 \oplus D_7$
 $P_4 = D_5 \oplus D_6 \oplus D_7$

[3] (20 marks)

[3A] (10+5=15 marks) A modified single-error correcting, double-error detecting Hamming code with four bits of Data $D_3, D_5, D_6,$ and D_7 has the following parity bit equations: $P_1 = D_3 \oplus D_5 \oplus D_7, P_2 = D_3 \oplus D_6 \oplus D_7, P_4 = D_5 \oplus D_6 \oplus D_7.$

a) Find the binary values of the four check bits for a single error in each of the eight bit code. Form a table.

$C_1 = P_1 \oplus D_3 \oplus D_5 \oplus D_6$ (1)
 $C_2 = P_2 \oplus D_3 \oplus D_5 \oplus D_7$ (1)
 $C_4 = P_4 \oplus D_3 \oplus D_6 \oplus D_7$ (1)
 $C_8 = P_8 \oplus D_5 \oplus D_6 \oplus D_7$ (1)

Error Bit	C_8	C_4	C_2	C_1	
1	0	0	0	1	(0.5)
2	0	0	1	0	(0.5)
3	0	1	1	1	(1)
4	0	1	0	0	(0.5)
5	1	0	1	1	(1)
6	1	1	0	1	(1)
7	1	1	1	0	(1)
8	1	0	0	0	(0.5)

$P_1 \ P_2 \ D_3 \ P_4 \ D_5 \ D_6 \ D_7 \ P_8$

b) For each of the following words read from memory evaluate the check bits and indicate error, double error, or no error has occurred. Write the correct word were possible.

i) 10100011
 $C_8 \ C_4 \ C_2 \ C_1 = 0000 \Rightarrow$ No error (1)

ii) 11001110
 $C_8 \ C_4 \ C_2 \ C_1 = 1011 \Rightarrow$ error in bit 5 (1)
 Right word is: 11000110 (1)

iii) 00011101
 $C_8 \ C_4 \ C_2 \ C_1 = 1010 \Rightarrow$ double error (1)
 Since it is not in the above.

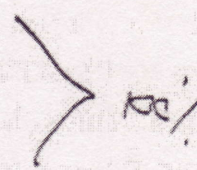
[3B] (3 marks) What are the limitations of the following techniques for detecting and in memory systems? (0.5 each)

- a) Error detection using single parity one bit
- b) Error correction using single parity none

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[4] (10+5+4=15 marks) We are interested in two implementations of a machine, one with special floating-point hardware. Both machines have a clock rate of 1000 MHz. Consider with the following mix of operations.

- floating-point multiply 10%
- floating-point add 15%
- floating-point divide 5%
- integer instructions 70%



Machine MFP (Machine with Floating Point) has floating point hardware and can execute the floating point instructions directly. It requires the following number of clock cycles for each class.

- floating-point multiply 6
- floating-point add 4
- floating-point divide 20
- integer instructions 2

Machine MNFP (Machine Without Floating Point) has no floating-point hardware and executes the floating-point operations using integer instructions. The integer instructions all take 2 clock cycles. The number of integer instructions needed to implement each of the floating-point operations is as follows:

- floating-point multiply 30
- floating-point add 20
- floating-point divide 50

a) Find the MIPS ratings for both machines. $MIPS = \frac{Inst\ Count}{Exec_time \cdot 10^6} = \frac{Inst\ Count}{CPI \cdot 10^6}$

$MIPS = \frac{clock\ rate}{CPI \times 10^6}$

$CPI\ for\ MFP = (10 \times 6 + 15 \times 4 + 5 \times 20 + 70 \times 2) / 100 = 3.6$ (2) Ave

$CPI\ for\ MNFP = 2$ (2)

$MIPS\ for\ MFP = \frac{1000\ M}{3.6 \cdot 10^6} = 278$ (2) and $MIPS\ for\ MNFP = \frac{1000\ M}{2 \cdot 10^6} = 500$

b) If the machine MFP needs 300 million instructions for this program, how many integer instructions does the machine MNFP require for the same program?

Instruction Class	Frequency on MFP	Count on MFP $\times 10^6$	Count on MNFP
Floating Point Multiply	10%	30	900
Floating Point Add	15%	40	900

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[6] (20 marks)

[6A] (10 marks) A program repeatedly performs a three-step process: It reads in a 4 Kb disk, does some processing on that data, and then writes out the result as another 4 K on the disk. Each block is located on a single track on the disk. The disk rotates at 5400 rpm, and has an average seek time of 8 ms, and has a transfer rate of 20 Mb/sec. The controller overhead program is using the disk or processor, and there is no overlapping of disk operation with processing step takes 20 million clock cycles, and the clock rate is 400 MHz. What is the speed of the system in blocks processed per second.

$$\text{Average rotation time} = \frac{0.5 \text{ rotations}}{5400 \frac{\text{rotations}}{\text{minute}} \cdot \frac{\text{minute}}{60 \text{ Seconds}}} = \underline{5.56 \text{ ms}}$$

$$\text{Transfer time} = \frac{4 \text{ Kb}}{20 \text{ Mb/sec}} = \underline{0.2 \text{ ms}} \quad (2)$$

$$\Rightarrow \text{Average disk access time} = 8 \text{ ms} + 5.56 \text{ ms} + 0.2 \text{ ms} + 2$$

Since each block processed involves two accesses (read & write) disk component of time is $2 \times 15.76 = \underline{31.52 \text{ ms}}$ (1)

$$\text{Computation takes } 20 \text{ million cycles} \times \frac{1}{400 \text{ MHz}} = \underline{50 \text{ ms}}$$

Thus, total time to process one block is $50 + 31.52 = \underline{81.52 \text{ ms}}$

Number of blocks processed per second is

$$1/0.08152 = \underline{12.27} \quad (1)$$

[6B] (6 marks) For the following set of variables, {CPI, clock rate (F), cycle time (T), instructions in program (I), number of cycles in program (C)}, identify all of the subsets to calculate execution time. Each subset should be minimal; that is, it should not contain that is not needed. ✓

- a) F, C (1)
 b) T, C (1)
 c) MIPS, I (1)
 d) CPI, C, MIPS (1)
 e) CPI, I, F (1)
 f) CPI, I, T (1)

$$\text{CPI} \equiv \frac{\text{cycles}}{\text{instructions}}$$