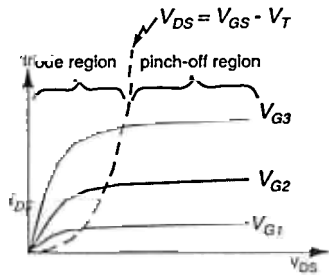


Transistor Characteristics (N Channel)



Simple Square Law Equations

Triode: $I_{DS} = k_p \frac{W}{L} \left(V_{GS} - V_T - \frac{V_{DS}}{2} \right) V_{DS}$ $V_{DS} < V_{GS} - V_T$

Pinch Off: $I_{DS} = \frac{k_p}{2} \frac{W}{L} (V_{GS} - V_T)^2$ $V_{DS} > V_{GS} - V_T$

(use $|V|$ for pmos) $|I_{DS}|_p = \frac{k_{pp}}{2} \left(\frac{W}{L} \right)_p (|V_{GS}| - |V_T|)^2$

$K_{pn} = \frac{\mu_n \epsilon_{ox}}{t_{ox}} = \mu_n C_{ox}$ $K_{pp} = \frac{\mu_p \epsilon_{ox}}{t_{ox}} = \mu_p C_{ox}$

Channel Length Modulation slope factor λ : $\frac{\Delta I_D}{I_D} = \lambda \Delta V_{DS}$, $\lambda \approx 1/L$.

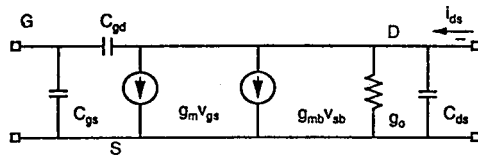
Transistor equations including channel length modulation:

Triode: $I_{DS} = K_p \frac{W}{L} \left(V_{GS} - V_T - \frac{V_{DS}}{2} \right) V_{DS} (1 + \lambda V_{DS})$ Pinch Off: $I_{DS} = \frac{K_p}{2} \frac{W}{L} (V_{GS} - V_T)^2 (1 + \lambda V_{DS})$

Body Effect γ - nonzero V_{SB} changes the threshold voltage as:

$V_T = V_{T0} + \gamma [\sqrt{2|\phi_F| + V_{SB}} - \sqrt{2|\phi_F|}]$ typically $2|\phi_F| = 0.7$ V Result: threshold is increased

Small Signal Parameters in Pinch-Off

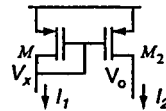
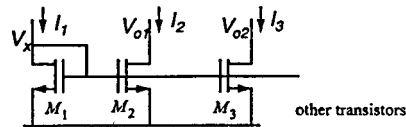


$g_m = \frac{dI_{DS}}{dV_{GS}} = \sqrt{2k_p \frac{W}{L} I_{DS}} = k_p \frac{W}{L} v_{ov}$

$g_o = \lambda I_D$ $\lambda \propto \frac{1}{L}$

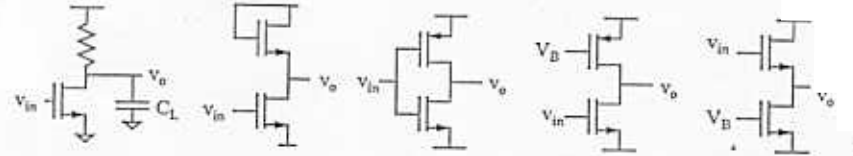
Diode Connection and Current Mirrors: Diode Connection: as M_1 below, connect drain and gate, hence

$V_{DS} = V_{GS}$. If $V_{DS} > V_T$, then always in pinch off. Small signal model with $g = g_m + g_o$.



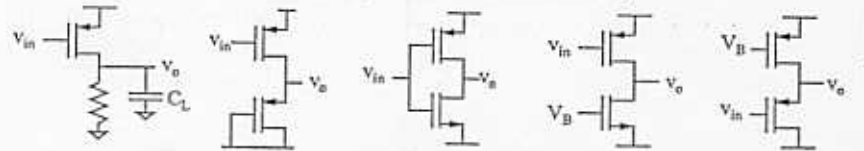
Current Mirror: $I_2 = I_1$ if $v_{o1} = v_x$. Otherwise currents will not match exactly because of output impedance e.g., at v_{o1} it is given by r_o of M_2 . Can increase by using cascode or other types of mirrors.

Gain Stages (Shown with NMOS Drivers)



Resistive Load: $\frac{v_o}{v_{in}} = \frac{g_m}{g_L + g_{ds}}$ Diode Load: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{m2} + g_{ds1} + g_{ds2}}$ Digital Style: $\frac{v_o}{v_{in}} = \frac{g_{m1} + g_{m2}}{g_{ds1} + g_{ds2}}$ Current Source Load: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{ds1} + g_{ds2}}$ Source Follower: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{m1} + g_{ds1}}$

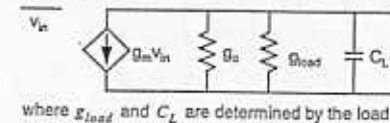
Gain Stages (Shown with PMOS Drivers)



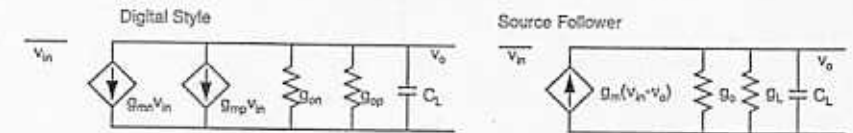
Resistive Load: $\frac{v_o}{v_{in}} = \frac{g_m}{g_L + g_{ds}}$ Diode Load: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{m2} + g_{ds1} + g_{ds2}}$ Digital Style: $\frac{v_o}{v_{in}} = \frac{g_{m1} + g_{m2}}{g_{ds1} + g_{ds2}}$ Current Source Load: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{ds1} + g_{ds2}}$ Source Follower: $\frac{v_o}{v_{in}} = \frac{g_{m1}}{g_{m1} + g_{ds1}}$

Small Signal Model

The gain of each, except for the last two is $\frac{g_m}{g_{eq}}$ where $g_{eq} = g_m + g_{load}$, and model is as below



where g_{load} and C_L are determined by the load



low frequency gain = $\frac{(g_{mn} + g_{mp})}{g_{eq}}$

low frequency gain = $\frac{g_m}{g_m + g_{eq}} = 1$

Slew Rate . Use current into capacitor, calculate $i = C \frac{\Delta v}{\Delta t}$ where $\frac{\Delta v}{\Delta t}$ is the slew rate.

Pole Frequency. $\omega_p = \frac{1}{r_{eq} C}$ where $r_{eq} = \frac{1}{g_{eq}}$ Unity Gain Bandwidth: $UGBW = \frac{g_m}{C_L}$

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